

Improving predictions for associated $t\bar{t}H$ production at the LHC: soft gluon resummation through NNLL accuracy

Anna Kulesza

Institute for Theoretical Physics, WWU Münster, D-48149 Münster, Germany

E-mail: anna.kulesza@uni-muenster.de

Leszek Motyka

Institute of Physics, Jagellonian University, S.Łojasiewicza 11, 30-348 Kraków, Poland

E-mail: leszekm@th.if.uj.edu.pl

Tomasz Stebel*

Institute of Nuclear Physics PAN, Radzikowskiego 152, 31-342 Kraków, Poland

E-mail: tomasz.stebel@uj.edu.pl

Vincent Theeuwes

Department of Physics, SUNY Buffalo, 261 Fronczak Hall, Buffalo, NY 14260-1500, USA

E-mail: vtheeuwes@buffalo.edu

In the following we present our recent results on the resummation of soft gluon corrections to the $pp \rightarrow t\bar{t}H$ cross section at the LHC. The resummation was carried out at next-to-next-to-leading-logarithmic (NNLL) accuracy using the Mellin space technique. Obtained results were matched to the NLO cross section. We show that the resummation leads to reduction of scale-variation uncertainty of the total $pp \rightarrow t\bar{t}H$ cross section.

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1. Introduction

Establishing the properties of the Higgs boson couplings to the Standard Model particles is one of the main tasks of the LHC experiment [1]. The associated production $t\bar{t}H$ offers a direct way to probe the strength of the top–Higgs Yukawa coupling and may be particularly sensitive to physics beyond the Standard Model. Therefore, the improvement of the accuracy for the theoretical predictions is of the central importance. The next-to-leading-order (NLO) QCD predictions were obtained some time ago [2, 3], later they were recalculated and matched to parton showers [4, 5, 6, 7]. Also the QCD-electro weak corrections were calculated [8, 9]. Finally, the NLO EW and QCD corrections to the hadronic $t\bar{t}H$ production with off-shell top and antitop quarks were obtained [10, 11]. The NNLO QCD analysis is currently out of reach so the calculation of soft gluon emission corrections is one of the best way to improve theoretical predictions. In Ref. [12] we presented the first calculation of the resummed total cross section for the $t\bar{t}H$ production at the next-to-leading-logarithmic (NLL) accuracy. The calculation relied on application of the traditional Mellin-space resummation formalism in the absolute threshold limit, i.e. in the limit of the partonic energy $\sqrt{\hat{s}}$ approaching the production threshold $M = 2m_t + m_H$. Subsequently we have performed [13] resummation of NLL corrections arising in the limit of $\sqrt{\hat{s}}$ approaching the invariant mass threshold Q , where $Q^2 = (p_t + p_{\bar{t}} + p_H)^2$. Recently we extended this calculation to the next-to-next-to-leading-logarithmic (NNLL) accuracy [14]. Threshold resummation can be also performed in the framework of the soft-collinear effective theory (SCET). For the $t\bar{t}H$ process this approach was first applied in Ref. [15] obtaining approximate NNLL and later full NNLL [16] accuracy.

In this note we report the threshold resummation in the invariant mass limit at the NNLL accuracy using the direct QCD Mellin-space approach [17]. Taking the Mellin transform allows one to systematically treat the logarithmic terms of the form $\alpha_s^n [\log^m(1-\rho)/(1-\rho)]_+$, with $m \leq 2n-1$ and $\rho = Q^2/\hat{s}$, appearing in the perturbative expansion of the partonic cross section to all orders in α_s . In Mellin space these logarithms turn into logarithms of the variable N , and the threshold limit $z \rightarrow 1$ corresponds to the limit $N \rightarrow \infty$. The Mellin moments of the cross section are taken w.r.t. the variable $\rho = Q^2/\hat{s}$: $\hat{\sigma}(N, Q^2) = \int_0^1 d\rho \rho^{N-1} \hat{\sigma}(\rho, Q^2)$.

We present numerical prediction for the NNLL resummed cross sections matched to the fixed order NLO results. In particular, we study the difference between the NNLL results and the NNLL results with a colour-averaging approximation of the hard function.

2. Resummation at invariant mass threshold

The resummed cross section in the Mellin space has the form [18]

$$\begin{aligned} \frac{d\tilde{\sigma}_{ij \rightarrow kLB}^{(\text{res})}}{dQ^2}(N, Q^2, \mu_F^2, \mu_R^2) &= \text{Tr} [\mathbf{H}_{ij \rightarrow kLB}(Q^2, \mu_F^2, \mu_R^2) \mathbf{S}_{ij \rightarrow kLB}(N+1, Q^2, \mu_F^2, \mu_R^2)] \\ &\times \Delta^i(N+1, Q^2, \mu_F^2, \mu_R^2) \Delta^j(N+1, Q^2, \mu_F^2, \mu_R^2), \end{aligned} \quad (2.1)$$

where $\mathbf{H}_{ij \rightarrow kLB}$ indicates the hard-scattering contributions (including phase space factor), $\mathbf{S}_{ij \rightarrow kLB}$ contains a soft wide-angle emission corrections and function $\Delta^i(\Delta^j)$ sums the softcollinear and collinear contributions from the incoming parton i (parton j) [19]. The trace in (2.1) is taken over colour space.

The soft function is given by a solution of the renormalization group equation [20, 21]:

$$\mathbf{S}_{ij \rightarrow klB}(N, Q^2, \mu_F^2, \mu_R^2) = \bar{\mathbf{U}}_{ij \rightarrow klB}(N, Q^2, \mu_F^2, \mu_R^2) \tilde{\mathbf{S}}_{ij \rightarrow klB}(\alpha_s(Q^2/\bar{N}^2)) \mathbf{U}_{ij \rightarrow klB}(N, Q^2, \mu_F^2, \mu_R^2), \quad (2.2)$$

where $\tilde{\mathbf{S}}_{ij \rightarrow klB}$ plays a role of a boundary condition.

Both hard function and soft matrix initial condition can be calculated perturbatively [20, 22]: $\mathbf{H}_{ij \rightarrow klB} = \mathbf{H}_{ij \rightarrow klB}^{(0)} + \frac{\alpha_s}{\pi} \mathbf{H}_{ij \rightarrow klB}^{(1)} + \dots$ and $\tilde{\mathbf{S}}_{ij \rightarrow klB} = \tilde{\mathbf{S}}_{ij \rightarrow klB}^{(0)} + \frac{\alpha_s}{\pi} \tilde{\mathbf{S}}_{ij \rightarrow klB}^{(1)} + \dots$. At the NNLL accuracy knowledge of $\tilde{\mathbf{S}}_{ij \rightarrow klB}^{(1)}$ and $\mathbf{H}_{ij \rightarrow klB}^{(1)}$ is required [23, 24] whereas for NLL only leading terms $\mathbf{H}_{ij \rightarrow klB}^{(0)}$, $\tilde{\mathbf{S}}_{ij \rightarrow klB}^{(0)}$ are needed. Hard function $\mathbf{H}_{ij \rightarrow klB}$ carries no dependence on N . The dependence on N in the soft function $\tilde{\mathbf{S}}_R$ enters only through the argument of α_s and (after expanding in α_s) results in $\alpha_s^2(\mu_R^2) \log N$ term.

The soft function evolution matrices $\mathbf{U}_{ij \rightarrow klB}$, $\bar{\mathbf{U}}_{ij \rightarrow klB}$ contain logarithmic enhancements due to soft wide-angle emissions [25]. $\mathbf{U}_{ij \rightarrow klB}$ is defined as a path-ordered exponent

$$\mathbf{U}_{ij \rightarrow klB}(N, Q^2, \mu_F^2, \mu_R^2) = \text{Pexp} \left[\int_{\mu_F}^{Q/\bar{N}} \frac{dq}{q} \mathbf{\Gamma}_{ij \rightarrow klB}(\alpha_s(q^2)) \right],$$

where the soft anomalous dimension is calculated as a perturbative function in α_s , $\mathbf{\Gamma}_{ij \rightarrow klB}(\alpha_s) = (\frac{\alpha_s}{\pi}) \mathbf{\Gamma}_{ij \rightarrow klB}^{(1)} + (\frac{\alpha_s}{\pi})^2 \mathbf{\Gamma}_{ij \rightarrow klB}^{(2)} + \dots$ [12, 26]. In order to diagonalize the one-loop soft anomalous dimension matrix we make use of the transformation [25]:

$$\mathbf{\Gamma}_R^{(1)} = \mathbf{R}^{-1} \mathbf{\Gamma}_{ij \rightarrow klB}^{(1)} \mathbf{R} \quad (2.3)$$

and other matrices are transformed using diagonalization matrix \mathbf{R} : $\mathbf{\Gamma}_R^{(2)} = \mathbf{R}^{-1} \mathbf{\Gamma}_{ij \rightarrow klB}^{(2)} \mathbf{R}$, $\mathbf{H}_R = \mathbf{R}^{-1} \mathbf{H}_{ij \rightarrow klB} (\mathbf{R}^{-1})^\dagger$, $\tilde{\mathbf{S}}_R = \mathbf{R}^\dagger \tilde{\mathbf{S}}_{ij \rightarrow klB} \mathbf{R}$. In the \mathbf{R} -representation the evolution factor \mathbf{U}_R (similarly $\bar{\mathbf{U}}_R$) can be written at NNLL accuracy as [27, 28]:

$$\mathbf{U}_R(N, Q^2, Q^2, \mu_R^2) = \left(\mathbf{1} + \frac{\alpha_s(\mu_R^2)}{\pi[1 - 2\alpha_s(\mu_R^2)b_0 \log N]} \mathbf{K} \right) \left[e^{g_s(N) \vec{\lambda}^{(1)}} \right]_D \left(\mathbf{1} - \frac{\alpha_s(\mu_R^2)}{\pi} \mathbf{K} \right), \quad (2.4)$$

where $K_{IJ} = \delta_{IJ} \lambda_I^{(1)} \frac{b_1}{2b_0^2} - \frac{(\mathbf{\Gamma}_R^{(2)})_{IJ}}{2\pi b_0 + \lambda_I^{(1)} - \lambda_J^{(1)}}$ and $\lambda_I^{(1)}$ are the eigenvalues of $\mathbf{\Gamma}_{ij \rightarrow klB}^{(1)}$. By $\left[e^{g_s(N) \vec{\lambda}^{(1)}} \right]_D$ we have denoted diagonal matrix with exponentiated eigenvalues on diagonal and $g_s(N)$ is a function which resums logarithms of N (see [14] for expression), b_0 and b_1 are the first two coefficients of expansion β_{QCD} in α_s .

The resummation-improved cross sections for the $pp \rightarrow t\bar{t}H$ process are obtained through matching the resummed expression with the full NLO cross sections

$$\frac{d\sigma_{h_1 h_2 \rightarrow klB}^{(\text{matched})}}{dQ^2}(Q^2, \mu_F^2, \mu_R^2) = \frac{d\sigma_{h_1 h_2 \rightarrow klB}^{(\text{NLO})}}{dQ^2}(Q^2, \mu_F^2, \mu_R^2) + \frac{d\sigma_{h_1 h_2 \rightarrow klB}^{(\text{res-exp})}}{dQ^2}(Q^2, \mu_F^2, \mu_R^2) \quad (2.5)$$

with

$$\frac{d\sigma_{h_1 h_2 \rightarrow klB}^{(\text{res-exp})}}{dQ^2} = \sum_{i,j} \int_C \frac{dN}{2\pi i} \rho^{-N} f_{i/h_1}^{(N+1)} f_{j/h_2}^{(N+1)} \left[\frac{d\tilde{\sigma}_{ij \rightarrow klB}^{(\text{res})}}{dQ^2} - \frac{d\tilde{\sigma}_{ij \rightarrow klB}^{(\text{res})}}{dQ^2} \Big|_{(\text{NLO})} \right], \quad (2.6)$$

\sqrt{S} [TeV]	μ_0	NLO [fb]	NLO+NLL[fb]	NLO+NNLL $\bar{\mathcal{C}}$ [fb]	NLO+NNLL[fb]
14	Q	$506^{+11.8\%}_{-11.5\%}$	$530^{+9.8\%}_{-9.2\%}$	$598^{+7.8\%}_{-7.3\%}$	$603^{+7.8\%}_{-6.9\%}$
	$Q/2$	$566^{+9.9\%}_{-10.6\%}$	$576^{+8.7\%}_{-8.0\%}$	$600^{+6.1\%}_{-7.0\%}$	$602^{+6.0\%}_{-6.4\%}$
	$M/2$	$604^{+6.1\%}_{-9.2\%}$	$609^{+8.4\%}_{-7.8\%}$	$609^{+6.9\%}_{-6.9\%}$	$607^{+5.7\%}_{-6.1\%}$

Table 1: Total cross section predictions for $pp \rightarrow t\bar{t}H$ at various central scale choices and resummation accuracies. The listed error is the theoretical error due to scale variation calculated using the 7-point method.

where $d\tilde{\sigma}_{ij \rightarrow kLB}^{(\text{res})}/dQ^2$ is given by (2.1) and $d\tilde{\sigma}_{ij \rightarrow kLB}^{(\text{res})}/dQ^2|_{(\text{NLO})}$ represents its perturbative expansion truncated at NLO. $f_{i/h}^{(N)}$ is a Mellin moment (with respect of x variable) of parton distribution function for parton i in hadron h .

Apart from the full NNLL cross sections we also consider the NLL results, obtained by taking $\mathbf{H}_{ij \rightarrow kLB} = \mathbf{H}_{ij \rightarrow kLB}^{(0)}$, $\tilde{\mathbf{S}}_{ij \rightarrow kLB} = \tilde{\mathbf{S}}_{ij \rightarrow kLB}^{(0)}$, $\mathbf{K} = \mathbf{0}$ and dropping NNLL terms in Δ and g_s . Additionally, we study the NNLL results where an approximation to the non-logarithmic terms, forgoing the colour structure of the one-loop hard corrections, has been applied. In this approximation, to which we refer as "NNLL $\bar{\mathcal{C}}$ ", we calculate a hard coefficient $\bar{\mathcal{C}}^{(1)}$ as a colour average of $\mathcal{O}(\alpha_s)$ non-logarithmic contributions:

$$\bar{\mathcal{C}}_{ij \rightarrow kLB}^{(1)}(Q^2, \mu_F^2, \mu_R^2) = \text{Tr} \left[\mathbf{H}_R^{(1)} \tilde{\mathbf{S}}_R^{(0)} + \mathbf{H}_R^{(0)} \tilde{\mathbf{S}}_R^{(1)} \right] / \text{Tr} \left[\mathbf{H}_R^{(0)} \tilde{\mathbf{S}}_R^{(0)} \right] \quad (2.7)$$

Because of the form of $\tilde{\mathbf{S}}^{(0)}$ [14], the one-loop hard coefficient $\bar{\mathcal{C}}^{(1)}$ involves only virtual hard contributions summed over colour channels. Accounting for the $\bar{\mathcal{C}}^{(1)}$ coefficient, Eq. (2.1) is then transformed into (we skip arguments for simplicity and write it in \mathbf{R} -representation):

$$\frac{d\tilde{\sigma}_{ij \rightarrow kLB}^{(\text{NNLL } \bar{\mathcal{C}})}}{dQ^2} = \left(1 + \frac{\alpha_s}{\pi} \bar{\mathcal{C}}_{ij \rightarrow kLB}^{(1)} \right) \text{Tr} \left[\mathbf{H}_R^{(0)} \bar{\mathbf{U}}_R \tilde{\mathbf{S}}_R^{(0)} \mathbf{U}_R \right] \Delta^i \Delta^j. \quad (2.8)$$

3. Numerical results

In this section we present our numerical results obtained for $\sqrt{S} = 14$ TeV. Results for the total cross section are obtained by integrating out the invariant mass distribution (2.5) over invariant mass Q . We use $m_t = 173$ GeV, $m_H = 125$ GeV and PDF4LHC15_100 sets [29]. The NLO cross section is calculated using the aMC@NLO code [30]. For the evaluation of the first-order hard function matrix $\mathbf{H}_{ij \rightarrow kLB}^{(1)}$ the one-loop virtual corrections to the process (decomposed into various colour transitions IJ) are required. We extract them numerically by modification of the publicly available POWHEL implementation of the $t\bar{t}H$ process [6].

Two choices for the central value of the renormalization and factorization scales are used: $\mu_0 = \mu_{F,0} = \mu_{R,0} = Q$ and $\mu_0 = \mu_{F,0} = \mu_{R,0} = M/2 = m_t + m_H/2$. The former choice is motivated by invariant mass Q being the natural scale for the invariant mass kinematics used in resummation. The latter choice of the scale is often made in the NLO calculations, see e.g. [2].

In Table 1 we show our numerical predictions for the total cross sections for three scale choices: $\mu_0 = Q$, $\mu_0 = M/2$ and ‘in-between’ value of $\mu_0 = Q/2$. The theoretical error due to

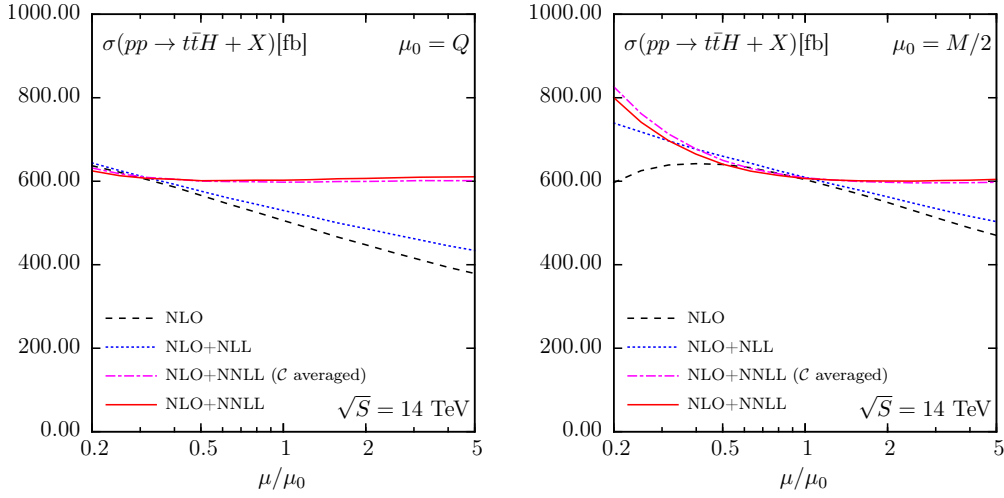


Figure 1: Scale dependence of the total cross section for the process $pp \rightarrow t\bar{t}H$ at the LHC with $\sqrt{S} = 14$ TeV. Results shown for the choice $\mu = \mu_F = \mu_R$ and two central scale values $\mu_0 = Q$ (left plot) and $\mu_0 = M/2$ (right plot).

scale variation is calculated using the 7-point method¹. It can be seen that for all scale choices the theoretical error decreases when one improves the predictions by adding resummation. For example, for $\mu_0 = Q/2$ the theoretical precision of the NLO+NNLL prediction is improved by about 40% with respect to the NLO result, bringing the scale error calculated with the 7-point method down to less than 6.5% of the central cross section value. Comparing last two columns of Table 1 we can conclude that the averaging of non-logarithmic contributions and removing $\mathbf{H}_R^{(1)} \tilde{\mathbf{S}}_R^{(1)}$ term result in a difference of below 1%.

In Figure 1 we show the scale dependence of $t\bar{t}H$ total cross sections calculated with the factorization and renormalization scale kept equal, $\mu = \mu_F = \mu_R$. We observe a substantial increase in the stability of the cross section value w.r.t. scale variation as the accuracy of resummation improves from NLL to NNLL. The NLO+NNLL prediction is characterised by a very low scale dependence. The rise of the cross section at small scales (for $\mu_0 = M/2$) is driven by the fall of the expansion of resummed result $\text{NNLL}|_{\text{NLO}}$ (second term in Eq. (2.6)) and is a consequence of the relatively large scale dependence of NLO qg channel contribution. This contribution appears first at NLO so no resummation is performed for it. Even though the qg production channel is formally subleading w.r.t $q\bar{q}$ and gg channels, it carries a relatively large numerical significance at low scales [14, 15]. Furthermore, we see that the colour-averaging procedure introduced in Eqs. (2.7) and (2.8) has only a minimal impact on the numerical results, i.e. NNLL \mathcal{C} results provide a very good approximation of the full NNLL results.

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¹In 7-point method error is calculated from minimum and maximum values obtained with $(\mu_F/\mu_0, \mu_R/\mu_0) = (0.5, 0.5), (0.5, 1), (1, 0.5), (1, 1), (1, 2), (2, 1), (2, 2)$.

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